

The vibronic coupling between the  ${}^3A_2(n\pi^*)$  and the  ${}^3B_2(\pi\pi^*)$  states demonstrates, in contrast, a much larger influence on the out-of-plane susceptibility of the molecule. The energy minimum for the  ${}^3A_2(n\pi^*)$  state corresponds to an out-of-plane conformation which is stabilized with respect to the planar conformation by about  $500\text{ cm}^{-1}$  in the CASSCF calculation and by about  $1200\text{ cm}^{-1}$  in the UHF calculation.

The  ${}^3A_1(\pi\pi^*)$  state has been shown to be subject to a vibronic coupling which is qualitatively similar to that between the  ${}^3B_{1u}$  and the  ${}^3E_{1u}$  states of benzene. The effect of introducing two nitrogen atoms in the aromatic ring manifests itself most clearly in the stabilization of the quinoidal conformation corresponding to  $\varphi = 0^\circ$ ; the other two quinoidal conformations are  $630\text{ cm}^{-1}$  higher in energy, while the antiquinoidal conformations form the saddle points in the trough.

Finally, we have considered the description of the geometry changes in the  $n\pi^*$  states in relation to the nature of the  $\pi^*$  orbital to which a lone-pair electron is in first approximation excited. Taking into account as well previous results on the  ${}^3B_1(n\pi^*)$  state of pyridine, it has been shown that the structural response of the

molecule to an  $n\pi^*$  excitation correlates remarkably well with the nodal-plane structure of the  $\pi^*$  orbital. This structural response shows up partly in the elongation of bonds and partly in out-of-plane distortions. Though an  $n\pi^*$  state in azabenzenes by its intrinsic nature seems to be susceptible to out-of-plane deformations, the contribution of such out-of-plane distortions to the total geometry relaxation does not have to dominate the structural response to the excitation.

**Acknowledgment.** This work was supported by The Netherlands Foundation for Chemical Research (SON) with financial aid from The Netherlands Organization for Scientific Research (NWO). W.J.B. acknowledges the San Diego Supercomputer Center (SDSC) for a grant of computer time on the CRAY-YMP, The Netherlands Organization for Scientific Research (NWO) for a research fellowship, and the Koninklijke/Shell Co. for the award of a bursary. This work was completed while W.J.B. was a postdoctoral fellow in the group of Prof. Dr. B. E. Kohler at the University of California, Riverside.

Registry No. Pyrimidine, 289-95-2.

## Clusters of Phosphorus: A Theoretical Investigation

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**Abstract:** A variety of phosphorus clusters up to  $P_{28}$  has been studied with ab initio SCF and MP2 calculations. Many of the larger clusters are found to be energetically stable with respect to  $P_4$ . The more interesting clusters are characterized by their equilibrium structures and NMR chemical shieldings and partially characterized by vibrational spectra to facilitate detection of the molecules. A probable reaction scheme for the formation of red phosphorus from white phosphorus emerges, and possible structural units of red phosphorus are established.

### I. Introduction

"Precise molecular structure data for the various forms (of phosphorus) is still limited and although their inter-conversion can, in most cases, be carried out, many of the phenomena involved remain imperfectly understood".<sup>1</sup> Some of these gaps can now be filled with results from large-scale ab initio calculations. Previous attempts were directed toward small clusters up to  $P_8$ , which were suspected to be present in the vapor phase along with  $P_2$  and  $P_4$ . A notable theoretical contribution came from Jones and Hohl<sup>2</sup> who systematically explored clusters up to  $P_8$  with a simulated annealing technique based on the density functional method. Their most striking results are the prediction of a "cuneane"  $P_8$  molecule as the most stable cluster besides tetrahedral  $P_4$  and the prediction of a moderately stable  $P_6$  cluster with  $C_{2v}$  symmetry formed by edge-on addition of  $P_2$  to  $P_4$ .

There is no experimental evidence for species other than  $P_2$  and  $P_4$  in the vapor phase obtained from white phosphorus between 300 and 1470 K.<sup>3a</sup> Cationic clusters up to at least  $P_{24}^+$  could be observed by mass spectroscopy in quenched vapor obtained from red phosphorus at 300K.<sup>3b</sup>

In this work we focus attention on even-membered larger phosphorus clusters up to  $P_{28}$ . Odd-membered clusters were not investigated, since our aim was to find phosphorus clusters and chain polymers which are energetically more stable than  $P_4$ , and

radicals are unlikely candidates. Three major types of clusters will be considered: isolated polyhedral clusters,  $P_4$  units linked by single bonds, and polyhedral units linked by two single bonds. From these investigations a consistent scheme of formation and structural features of red phosphorus emerges, which has some bearing on violet (Hittorf) phosphorus.<sup>4</sup> We further obtain hints for the possible existence of  $P_{12}$  and  $P_{16}$  clusters as new forms of phosphorus.

In our choice of potentially favorable structures we have been guided by chemical intuition and by a wealth of structures of substituted phosphanes<sup>5</sup> and polyphosphides.<sup>6</sup> However, some of those structural units do not lend themselves to medium-sized clusters. This includes the odd-membered subunits  $P_7$  and  $P_9$ , which can only occur in larger aggregates unless dangling bonds are saturated.

### II. Details of Computation

SCF and MP2 treatments as well as SCF force field calculations to compute vibrational frequencies have been carried out with the program system TURBOMOLE.<sup>7</sup> NMR shielding constants were computed by the SCF/GIAO method<sup>8</sup> with the program SHEILA,<sup>7b</sup> which uses a semidirect algorithm for the solution of coupled-perturbed Hartree-Fock (CPHF) equations for the magnetic field as perturbation.

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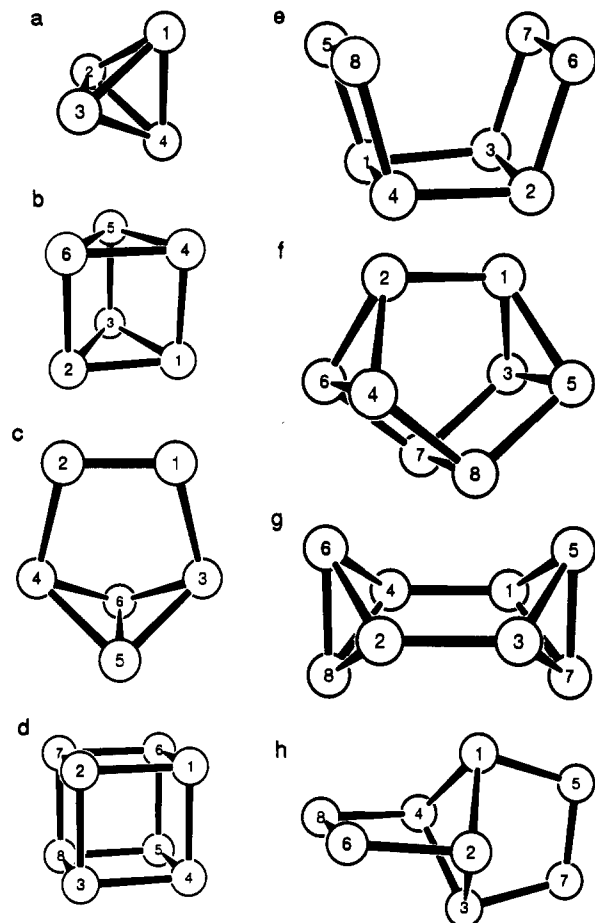
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**Figure 1.** Computed structures of phosphorus clusters  $P_4$  to  $P_8$ : (a)  $P_4$  ( $T_d$ ), (b)  $P_6$  ( $D_{3h}$ ), (c)  $P_6$  ( $C_{2v}$ ), (d)  $P_8$  ( $O_h$ ), (e)  $P_8$  ( $C_{2v}$ ) ladder-like; (f)  $P_8$  ( $C_{2v}$ ) cuneane-like, (g)  $P_8$  ( $D_{2h}$ ), (h)  $P_8$  ( $D_{2d}$ ).

Basis sets were taken from the new TURBOMOLE basis set library.<sup>9</sup> Three basis sets have been employed for P: split valence plus polarization SVP, {5311/511/1},  $\eta_d = 0.45$ ; double- $\zeta$  plus polarization DZP, {521111/31111/1},  $\eta_d = 0.45$ ; triple- $\zeta$  plus double polarization TZDP, {5121111/51111/11},  $\eta_d = 0.27$  and 0.8. For additional calculations on phosphanes  $P_3H_2$ ,  $P_3H_2$ , and  $P_{12}H_2$ , a {31} hydrogen basis was used.<sup>10</sup> The SCF structure optimizations, force field calculations, and MP2 treatments were carried out employing the SVP basis throughout. The TZDP basis was mainly used for smaller clusters ( $P_4$  and  $P_{12}$ ) to check the accuracy of the SVP basis. NMR chemical shifts were treated with DZP and (partly) TZDP basis sets. The calculations were carried out on workstations, IBM Risc 6000, partly with the parallel version<sup>11</sup> of TURBOMOLE using four workstations simultaneously.

### III. Energetics of Phosphorus Clusters

**The Smaller Clusters  $P_4$  to  $P_8$ .** Extensive ab initio calculations on tetrahedral  $P_4$ , Figure 1a, were aimed at an understanding of its remarkable stability,<sup>2,12</sup> which has few analogues in hydrocarbon chemistry. Today it is well established that inclusion of polarization functions in the basis set is mandatory for a meaningful description of electronic structure and stability of  $P_4$  — and other phosphorus clusters as well. Our calculations on  $P_4$  are only meant as a reference to which other phosphorus clusters will be compared.

The following discussions are based on the SCF/SVP energies collected in Table I; the accuracy of these results will be addressed in a later section.

The most stable six-membered cluster is not the prismane analogue  $P_6$  ( $D_{3h}$ ), Figure 1b, but the  $C_{2v}$  structure, Figure 1c, which can best be described as  $P_2$  added edge-on to  $P_4$  and con-

**Table I.** Computed SCF/SVP Energies of Phosphorus Clusters  $P_n$

mol	sym	fig	$E_{SCF}$ (au)	$\Delta E_n^a$	$\Delta E_n/(P_4)^b$
$P_4$	$T_d$	1a	-1362.544 49	0	0
$P_6$	$D_{3h}$	1b	-2043.779 39	+98	+65
$P_6$	$C_{2v}$	1c	-2043.784 07	+85	+57
$P_8$	$C_{2v}$	1e	-2725.016 63	+190	+95
$P_8$	$O_h$	1d	-2725.032 13	+149	+75
$P_8$	$D_{2d}$	1h	-2725.039 56	+130	+65
$P_8$	$D_{2h}$	1g	-2725.041 77	+124	+62
$P_8$	$C_{2v}$	1f	-2725.073 18	+42	+21
$P_{10}$	$C_{2v}$	4c	-3406.320 99	+106	+42
$P_{10}$	$C_{2h}$	7a	-3406.333 21	+74	+29
$P_{10}$	$C_{3v}$	3a	-3406.340 79	+54	+22
$P_{10}$	$C_2$	3h	-3406.345 98	+37	+15
$P_{10}$	$C_s$	4a	-3406.360 05	+3	+1
$P_{10}$	$C_{2v}$	6a	-3406.362 19	-3	-1
$P_{12}$	$D_{2d}$	5a	-4087.589 30	+116	+39
$P_{12}$	$C_{2v}$	4b	-4087.621 35	+32	+11
$P_{12}$	$C_s$	5b	-4087.627 71	+15	+5
$P_{12}$	$D_{3d}$	3b	-4087.645 51	-32	-11
$P_{14}$	$D_{3h}$	3c	-4768.868 47	+98	+28
$P_{14}$	$C_s$	6e	-4768.941 66	-94	-27
$P_{16}$	$D_{2h}$		-5450.118 28	+157	+39
$P_{16}$	$D_{4d}$	3d	-5450.138 68	+103	+26
$P_{16}$	$C_s$	7b	-5450.167 46	+28	+7
$P_{16}$	$C_s$	5c	-5450.172 49	+14	+4
$P_{16}$	$C_2$	6b	-5450.197 42	-51	-13
$P_{16}$	$C_{2h}$	5d	-5450.219 43	-109	-27
$P_{18}$	$D_{3h}$	3g	-6131.459 48	-24	-5
$P_{18}$	$C_{2v}$	6c	-6131.515 88	-172	-38
$P_{20}$	$C_{3v}$	3f	-6812.637 20	+224	+45
$P_{20}$	$I_h$	3e	-6812.638 92	+219	+44
$P_{24}$	$C_{2v}$	5e	-8175.318 78	-136	-23
$P_{28}$	$C_{2v}$	6d	-9537.933 14	-319	-46

<sup>a</sup>  $\Delta E_n = E_{SCF} - n/4 E_{SCF}(P_4)$  (kJ/mol). <sup>b</sup>  $\Delta E_n/(P_4) = \Delta E_n$  per  $P_4$  unit (kJ/mol).

taining a PP double bond. The present calculations confirm earlier results of Jones and Hohl.<sup>2</sup> Neither of the  $P_6$  clusters is energetically more stable than  $P_4$ . A functionalized  $P_6$  molecule,  $P_6Cp^*_2$ , with two pentamethylcyclopentadienyl rests added to the PP double bond in the  $P_6$  ( $C_{2v}$ ) structure has been characterized by X-ray structure analysis.<sup>13</sup>

Jones and Hohl<sup>2</sup> describe four structures of  $P_8$  of which the cubane analogue  $P_8$  ( $O_h$ ), Figure 1d, is among the least stable, Table I. One of the  $P_8$  structures ( $C_2$ ) found by the density functional method could not be reproduced at the SCF/SVP level: the structure relaxed to one with three fused four-membered rings and two PP double bonds, Figure 1e, which is even less stable than the cubane structure. The most stable  $P_8$  cluster is the cuneane analogue  $P_8$  ( $C_{2v}$ ), Figure 1f, for the first time identified by Jones and Hohl.<sup>2</sup> They found it to be more stable than  $2P_4$  by 46 kJ/mol but were cautious with this conclusion. Our SCF and MP2 calculations confirm this cuneane structure as the most stable  $P_8$  isomer, but we find it energetically less stable than  $2P_4$  by 42 kJ/mol. Another interesting geometry<sup>2</sup> is  $P_8$  ( $D_{2h}$ ), Figure 1g: two  $P_4$  units are added edge to edge. A third isomer of  $P_8$  which is more stable than the  $O_h$  structure is  $P_8$  ( $D_{2d}$ ), Figure 1h. This structure has not been found by simulated annealing based on the density functional method.<sup>2</sup> It shows two PP double bonds and can be obtained from  $P_6$  ( $C_{2v}$ ) by another edge-on addition of  $P_2$ . We conclude the following: no  $P_8$  cluster is stable with respect to  $2P_4$ ; the most stable  $P_8$  clusters are those with symmetries  $C_{2v}$  and  $D_{2h}$ .

**$P_4$  Units Linked by Single Bonds.** In 1952 Pauling and Simonetta<sup>14</sup> suggested that red phosphorus is formed from the white allotrope by breaking only a single bond in the  $P_4$  tetrahedron and then linking  $P_4$  units to an infinite chain. We have studied this possibility by calculations of  $P_4$  oligomers with hydrogen saturating the terminal dangling bonds. The computed energies are given in Table II.

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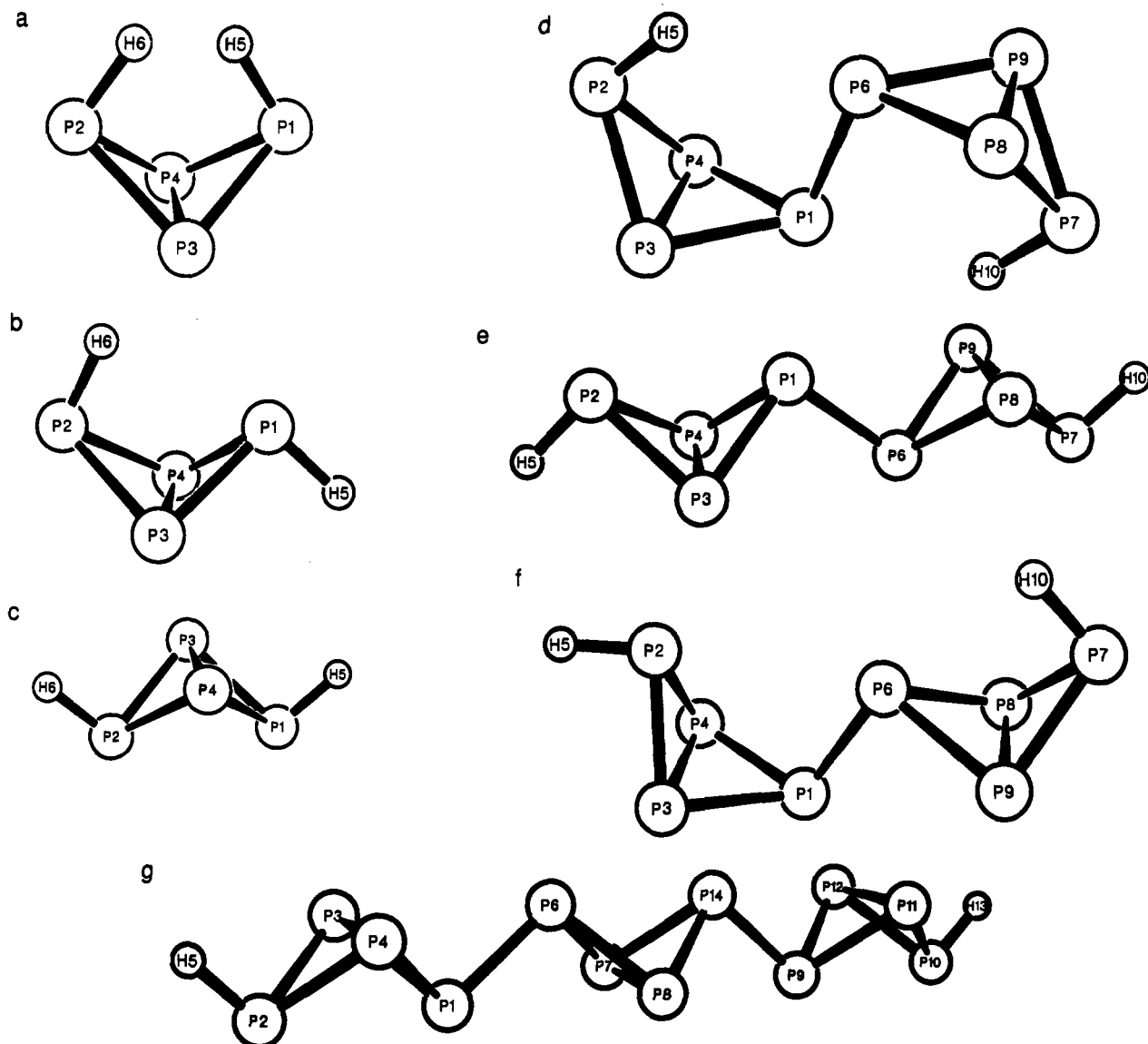
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**Figure 2.** Computed structures of  $H(-P_4)_n-H$  molecules: (a)  $P_4H_2$  ( $C_{2v}$ ) endo-endo, (b)  $P_4H_2$  ( $C_3$ ), (c)  $P_4H_2$  ( $C_{2v}$ ) exo-exo, (d)  $P_8H_2$  ( $C_{2h}$ ) all-endo, (e)  $P_8H_2$  ( $C_{2h}$ ) all-exo, (f)  $P_8H_2$  ( $C_s$ ), (g)  $P_{12}H_2$  ( $C_{2v}$ ).

**Table II.** Computed SCF/SVP Energies of  $P_4H_2$  Compounds

mol	sym	fig	$E_{SCF}$ (au)
$P_4H_2$	$C_{2v}$	2a	-1363.672 63
$P_4H_2$	$C_{2h}$	2b	-1363.678 84
$P_4H_2$	$C_{2v}$	2c	-1363.679 78
$P_8H_2$	$C_{2h}$	2d	-2726.194 62
$P_8H_2$	$C_{2h}$	2e	-2726.220 28
$P_8H_2$	$C_s$	2f	-2726.213 81
$P_{12}H_2$	$C_{2h}$	2g	-4088.760 81

The monomer,  $P_4H_2$ ,<sup>5,15</sup> comes in three stereoisomers: endo-endo, Figure 2a, endo-exo, Figure 2b, and exo-exo, Figure 2c. The endo-endo isomer is energetically unfavorable due to steric hindrance between the hydrogen atoms: the PPH bond angles are forced to open to  $100^\circ$ . The other two isomers are of comparable stability, with the exo-exo structure more stable at the SCF/SVP level. A previous treatment at the MP2 level using a 6-31G++(d,p) basis<sup>16</sup> has led to the same result. The substituted phosphane  $P_4R_2$  exists in the exo-exo form.<sup>15</sup>

The dimer  $P_8H_2$  resulting from the (unfavorable) endo-endo  $P_4H_2$  forms two (very similar) conformers of which the more symmetric conformer ( $C_{2h}$ ), Figure 2d, with the lone pairs in anti

position is more stable. Only a single structure could be located for the dimer arising from two exo-exo monomers, again in an anti conformation of the lone pairs ( $C_{2h}$ ), Figure 2e. This molecule is energetically favored over the dimer built from the endo-endo monomers by 67 kJ/mol. It can thus be concluded that an exo-exo linkage is preferred compared to an endo-endo linkage. We further studied the linkage of two endo-exo forms head to tail. The only stable geometry found is shown in Figure 2f (with  $C_s$  symmetry). This alternative is less stable than the exo-exo dimer and confirms that the exo-exo linkage of two  $P_4$  units with lone pairs in the anti position is most stable.

With these results for the energetics of isomers and conformers of  $P_4H_2$  and  $P_8H_2$  we restricted our study of  $P_{12}H_2$  to the isomer shown in Figure 2g, which has exo-exo linkages only and exhibits two trans conformations. The structural parameters of the central  $P_4$  unit vary very little from those in the terminal units, or from those in  $P_8H_2$ . We thus conclude that

$$E(-P_4-) - E(P_4) \approx E(P_{12}H_2) - E(P_8H_2) - E(P_4) = 10 \text{ kJ/mol} \quad (1)$$

is a good approximation of the energy per  $P_4$  unit in the polymer suggested by Pauling and Simonetta, which implies that  $(-P_4)_\infty$  is less stable than white phosphorus by about 10 kJ/mol ( $P_4$ ). Infinite chains of  $P_4$  (of this kind) are not a likely intermediate in the formation of red phosphorus and are probably not formed at all.

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**Table III.** Computed SCF (Harmonic Approximation) Zero Point Vibrational Energies (ZPVE) and MP2 Energy Contributions  $E_{\text{corr}}$  (All Core Electrons Frozen) Obtained with the SVP Basis

mol	sym	fig	$E_{\text{corr}}$ (au)	$\Delta E_n$ (kJ/mol) <sup>a</sup>	ZPVE (kJ/mol)
P <sub>4</sub>	T <sub>d</sub>	1a	-0.451 55	0	18
P <sub>6</sub>	D <sub>3h</sub>	1b	-0.661 73	+139	30
P <sub>6</sub>	C <sub>2v</sub>	1c	-0.680 66	+77	29
P <sub>8</sub>	O <sub>h</sub>	1d	-0.869 60	+237	42
P <sub>8</sub>	D <sub>2h</sub>	1g	-0.911 61	+101	
P <sub>8</sub>	C <sub>2v</sub>	1f	-0.904 48	+38	42
P <sub>8</sub>	D <sub>2d</sub>	1h	-0.903 66	+128	41
P <sub>10</sub>	C <sub>3v</sub>	3a	-1.127 81	+56	54
P <sub>10</sub>	C <sub>2</sub>	3h	-1.140 48	+10	54
P <sub>10</sub>	C <sub>2v</sub>	6a	-1.145 16	-45	53
P <sub>10</sub>	C <sub>s</sub>	4a	-1.143 56	-35	54
P <sub>12</sub>	C <sub>s</sub>	5b	-1.377 28	-44	
P <sub>12</sub>	D <sub>3d</sub>	3b	-1.375 26	-86	67
P <sub>14</sub>	C <sub>s</sub>	6e	-1.609 37	-170	
P <sub>16</sub>	C <sub>2h</sub>	5d	-1.845 38	-212	
P <sub>16</sub>	C <sub>2</sub>	6b	-1.840 02	-140	
P <sub>18</sub>	C <sub>2v</sub>	6c	-2.071 50	-276	
P <sub>20</sub>	I <sub>h</sub>	3e	-2.310 47	+81	110

<sup>a</sup>  $\Delta E_n = E - n/4E(P_4)$  (kJ/mol), computed reaction energies at the MP2 level.

**Table IV.** SCF and MP2 (All Core Electrons Frozen) Energies Computed with the Extended TZDP Basis at SCF/SVP Geometries

mol	sym	fig	$E_{\text{SCF}}$ (au)	$E_{\text{corr}}$ (au)	$\Delta E_{\text{SCF}}$ <sup>a</sup>	$\Delta E_{\text{MP2}}$ <sup>a</sup>
P <sub>4</sub>	T <sub>d</sub>	1a	-1363.020 65	-0.50227	0	0
P <sub>8</sub>	C <sub>2v</sub>	1f	-2726.020 01	-1.01185	+56	+36
P <sub>12</sub>	D <sub>3d</sub>	3b	-4089.061 11	-1.53250	+2	-66
P <sub>16</sub>	C <sub>2h</sub>	5d	-5452.105 70		-61	
P <sub>20</sub>	I <sub>h</sub>	3e	-6815.001 15		+268	

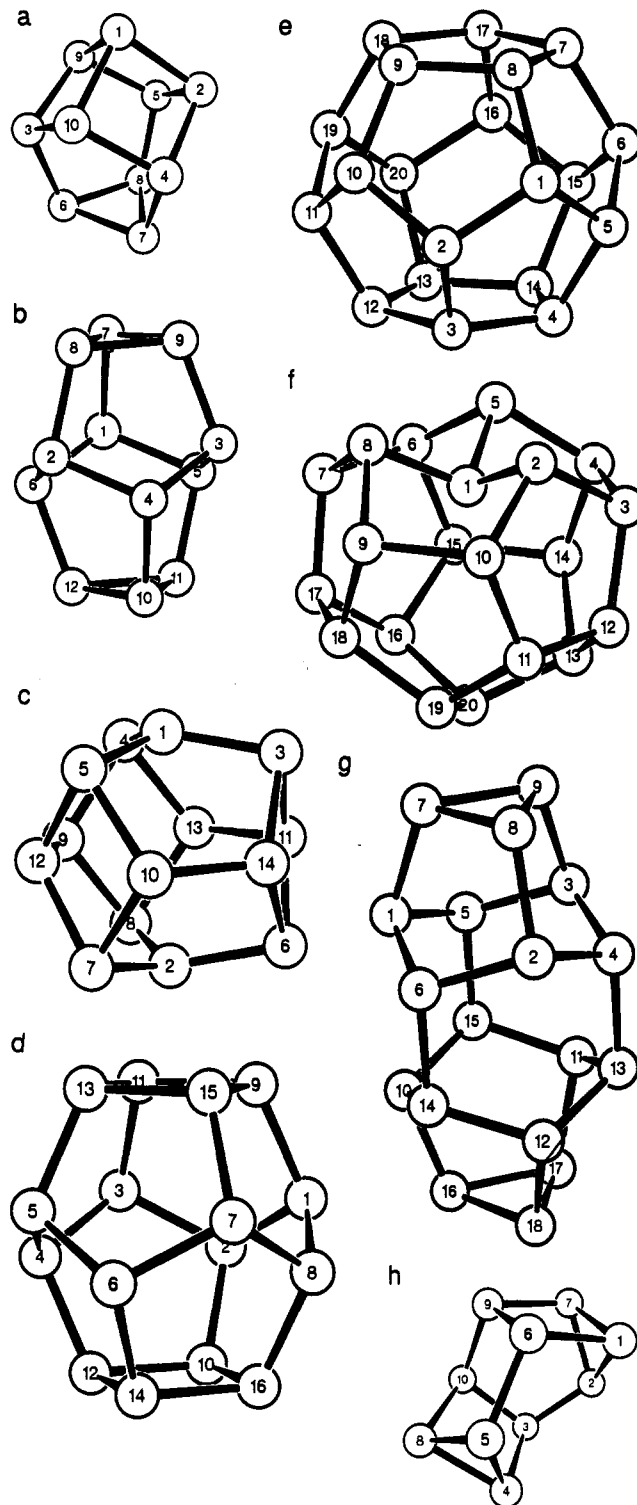
<sup>a</sup>  $\Delta E = E(P_n) - n/4E(P_4)$  (kJ/mol).

**Polyhedral Clusters P<sub>10</sub> to P<sub>20</sub>.** The energies of the clusters to be discussed now are collected in Table I. P<sub>10</sub> (C<sub>2</sub>), Figure 3h, is found to be comparable in stability to P<sub>8</sub> (C<sub>2v</sub>) and is unstable with respect to <sup>5</sup>/<sub>2</sub>P<sub>4</sub>. Slightly higher in energy is P<sub>10</sub> (C<sub>3v</sub>), Figure 3a. P<sub>12</sub> (D<sub>3d</sub>), Figure 3b, seems to be the most stable polyhedral phosphorus cluster. In particular it is more stable than P<sub>3</sub>P<sub>4</sub> within the SCF/SVP and MP2/SVP approximations. Six puckered five-membered rings with bond angles close to the preferred values between 95° and 100°, Table VI, provide an intuitive rationalization of this finding. To confirm our result we also performed single point SCF and MP2 calculations with the extended TZDP basis at the SCF/SVP geometry and included SCF/SVP zero point vibration effects (harmonic approximation). P<sub>12</sub> (D<sub>3d</sub>) is stable against dissociation into 3P<sub>4</sub> by 53 kJ/mol on this level, as shown in Table V. Computed properties of P<sub>12</sub> are documented in Table VI and are available as supplementary material.

The higher polyhedral clusters P<sub>14</sub> (D<sub>3h</sub>), Figure 3c, P<sub>16</sub> (D<sub>4d</sub>), Figure 3d, and the dodecahedral P<sub>20</sub> (I<sub>h</sub>), Figure 3e, were found to be unstable with respect to decomposition into P<sub>4</sub>. Reasons for this behavior may be the presence of four-membered rings, an increasingly planar coordination of phosphorus, and/or the increase in bond angles to 108° in P<sub>20</sub> (I<sub>h</sub>), which is unstable despite an all five-membered ring structure. Large bond angles are partly avoided in the C<sub>3v</sub> structure of P<sub>20</sub>, Figure 3f, where one phosphorus lone pair points into the polyhedron. This structure was found to be even less stable than the I<sub>h</sub> structure, Table I.

One higher polyhedral cluster, P<sub>18</sub> (D<sub>3h</sub>), Figure 3g, was found to be energetically more stable than P<sub>4</sub> at the SCF/SVP level but less stable than P<sub>12</sub> (D<sub>3d</sub>). The structure of P<sub>18</sub> may be related to that of P<sub>12</sub> (D<sub>3d</sub>): if one of the three-membered rings in P<sub>12</sub> is removed, and the resulting open P<sub>9</sub> cage is fused with another P<sub>9</sub> cage, one obtains P<sub>18</sub>. In comparison to P<sub>12</sub> it suffers again from too large bond angles.

**Phosphorus Clusters Containing PP Double Bonds.** Besides the smaller clusters P<sub>6</sub> (C<sub>2v</sub>), Figure 1c, and P<sub>8</sub> (D<sub>2d</sub>), Figure 1h (which originate from P<sub>4</sub> by adding one or two P<sub>2</sub> molecules, respectively), we also investigated three medium-sized clusters with PP double

**Figure 3.** Computed structures of polyhedral phosphorus clusters P<sub>10</sub> to P<sub>20</sub>: (a) P<sub>10</sub> (C<sub>3v</sub>), (b) P<sub>12</sub> (D<sub>3d</sub>), (c) P<sub>14</sub> (D<sub>3h</sub>), (d) P<sub>16</sub> (D<sub>4d</sub>), (e) P<sub>20</sub> (I<sub>h</sub>), (f) P<sub>20</sub> (C<sub>3v</sub>), (g) P<sub>18</sub> (D<sub>3h</sub>), (h) P<sub>10</sub> (C<sub>2</sub>).

bonds: P<sub>10</sub> (C<sub>s</sub>), Figure 4a, P<sub>12</sub> (C<sub>2v</sub>), Figure 4b, and P<sub>10</sub> (C<sub>2v</sub>), Figure 4c. These are obtained from the cuneane analogue P<sub>8</sub> (C<sub>2v</sub>) by adding P<sub>2</sub>.

P<sub>10</sub> (C<sub>s</sub>) is of comparable stability as P<sub>4</sub>, Table I. This surprise (in view of the PP double bond) can be rationalized as the release of ring strain from the two adjacent four-membered rings present in P<sub>8</sub> (C<sub>2v</sub>), a constellation which proved especially unfavorable in P<sub>8</sub> (O<sub>h</sub>). This interpretation is supported by the notion that a second P<sub>2</sub> molecule added to yield P<sub>12</sub> (C<sub>2v</sub>) leads to destabilization, Table I. The calculated properties of P<sub>10</sub> (C<sub>s</sub>) are given in Table VI and are available as supplementary material. We

**Table V.** Comparison of Reaction Energies Obtained at Various Levels of Approximation (in Parentheses: MP2 Contributions Only)

reaction <sup>a</sup>	fig	SVP		TZDP		TZDP MP2 + ZPVE <sup>b</sup>
		SCF	MP2	SCF	MP2	
1.5P <sub>4</sub> → P <sub>6</sub> (C <sub>2v</sub> )	1b	86	77 (-9)	96	88 (-9)	90
2P <sub>4</sub> → P <sub>8</sub> (C <sub>2v</sub> )	1f	42	38 (-4)	56	36 (-10)	42
3P <sub>4</sub> → P <sub>12</sub> (D <sub>3d</sub> )	3b	-32	-86 (-54)	2	-66 (-68)	-53
4P <sub>4</sub> → P <sub>16</sub> (C <sub>2h</sub> )	5d	-109	12 (-103)	-61		
5P <sub>4</sub> → P <sub>20</sub> (I <sub>h</sub> )	3e	219	-81 (-138)	268		

<sup>a</sup> Molecules are designated as shown in the corresponding figures. <sup>b</sup> ZPVE: zero point vibrational energies, taken from Table III.

**Table VI.** Computed SCF/SVP Bond Distances and Angles of the Most Stable Phosphorus Clusters<sup>a</sup>

mol	sym	fig	structural parameters
P <sub>4</sub>	T <sub>d</sub>	1a	1-2 218.9 (220.8)
P <sub>8</sub>	C <sub>2v</sub>	1f	1-2 222.5, 1-3 220.6, 3-5 229.2, 3-7 225.8, 7-8 222.8 4-8-5 105.9
P <sub>10</sub>	C <sub>2v</sub>	6a	1-2 221.5, 1-3 222.5, 3-5 221.5, 3-6 221.8, 5-6 222.4 3-1-8 100.3, 1-3-6 105.2, 3-5-4 92.9, 3-6-4 92.8
P <sub>10</sub>	C <sub>r</sub>	4a	1-2 224.5, 1-3 221.5, 2-4 223.6, 3-7 222.1, 3-10 224.9, 4-6 226.0, 4-8 225.2, 7-8 225.8, 9-10 201.4 1-2-4 106.7, 3-1-5 99.4, 1-3-10 99.7, 3-7-6 96.2
P <sub>12</sub>	D <sub>3d</sub>	3b	1-5 222.2 (221.1), 1-7 223.8 (221.6), 7-8 225.2 (228.0), 5-1-6 106.3 (106.9), 5-1-7 101.8 (101.5)
P <sub>14</sub>	C <sub>i</sub>	6e	1-2 224.1, 1-3 223.6, 2-4 222.1, 3-5 226.1, 3-7 225.0, 4-8 221.3, 4-10 222.6, 7-8 226.5, 9-10 225.1, 9-11 222.0, 11-13 221.4, 11-14 221.8, 13-14 222.8 2-1-3 106.6, 2-4-8 100.1, 4-2-6 99.6, 2-6-9 101.8, 6-9-11 100.2, 9-11-13 110.0, 11-13-12 93.2
P <sub>16</sub>	C <sub>2h</sub>	5d	1-2 225.0, 1-3 224.3, 2-4 221.5, 3-5 225.7, 3-7 225.1, 4-8 220.3, 4-13 224.0, 7-8 227.2 2-1-3 106.6, 4-2-6 105.6, 2-4-13 107.9, 7-6-14 104.4
P <sub>16</sub>	C <sub>2</sub>	6b	1-2 224.9, 1-3 226.6, 1-5 223.7, 4-6 223.3, 5-6 224.6, 5-7 222.1, 6-8 222.0, 8-9 222.5, 9-7 222.4, 7-10 221.2, 8-10 221.3, 9-10 222.4 1-2-4 86.7, 1-3-4 85.9, 2-1-5 100.6, 3-1-5 92.9, 2-4-6 100.8, 1-5-7 103.5, 4-6-8 103.6, 6-8-10 110.4, 7-10-8 93.5, 6-8-9 104.1
P <sub>18</sub>	C <sub>2v</sub>	6c	1-2 224.1, 1-3 223.7, 2-4 222.3, 3-5 226.2, 3-7 224.9, 4-8 221.6, 4-18 222.2, 7-8 226.5, 17-18 228.7 1-2-4 99.2, 2-4-8 100.0, 2-4-18 98.0, 8-4-18 98.0, 4-18-14 102.2
P <sub>28</sub>	C <sub>2v</sub>	6d	1-2 224.1, 1-3 223.7, 2-4 222.3, 3-5 226.3, 3-7 224.9, 4-8 221.6, 4-15 222.3, 7-8 226.6, 9-10 224.5, 9-24 229.9, 10-13 222.7, 10-14 220.9, 12-13 231.1, 14-15 227.4 1-2-4 99.2, 2-1-5 106.7, 2-4-15 102.4, 8-4-15 98.1, 11-9-24 99.4, 9-11-12 98.8, 4-15-11 101.6, 15-11-9 104.8

<sup>a</sup> Atoms are labeled as in corresponding figures. Bond distances are in pm and angles in deg. MP2/SVP results are given in parentheses as far as available.

note that P<sub>14</sub>R<sub>4</sub>, where organic rests R have been added to the double bonds, has been described in ref 5 (structure 67).

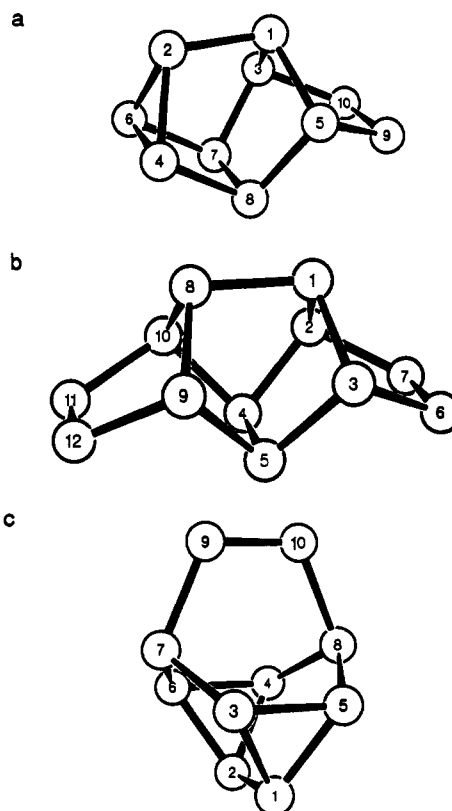
An isomeric form of P<sub>10</sub>, Figure 4c, where P<sub>2</sub> has been added to the bond fusing the two four-membered rings in P<sub>8</sub> (C<sub>2v</sub>), is found to be energetically much less favorable due to the five-membered rings now being forced into a near-planar conformation. Analogous structures will therefore not be considered further in this work.

**P<sub>4</sub> Units Linked by Two Single Bonds.** The smallest cluster of this type has already been mentioned: it is P<sub>8</sub> (D<sub>2h</sub>), Figure 1g, the dimer of tetrahedral P<sub>4</sub>. Having this structure in mind we introduce the mnemotechnic notation P<sub>4</sub>=P<sub>4</sub> for this molecule. The equal sign "=" indicates two single bonds which connect the two (distorted) tetrahedrons. Note that two bonds have to be broken and two bonds have to be formed to obtain P<sub>4</sub>=P<sub>4</sub> from 2P<sub>4</sub> while the nuclear rearrangement involved is small. For the energetics of the (endothermic) reaction consult Table I.

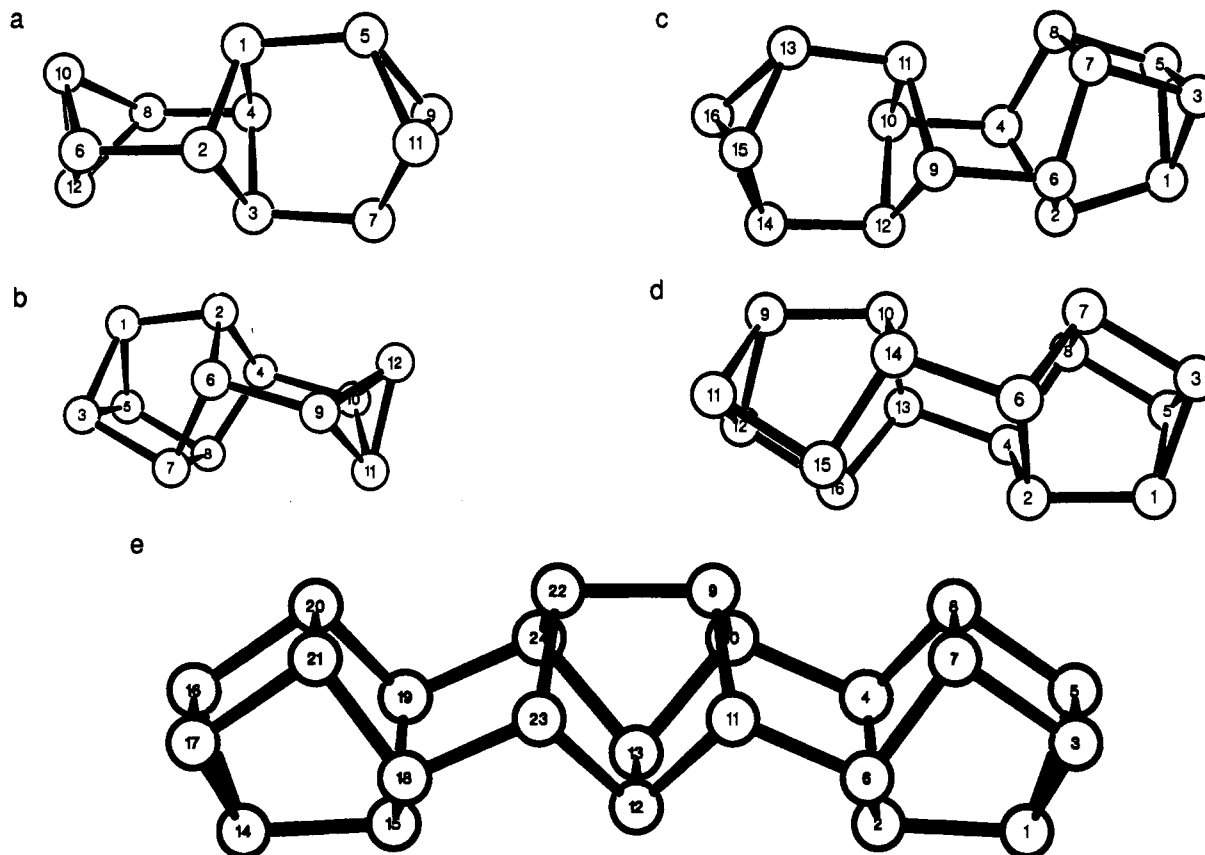
It is now possible to form oligomeric clusters of P<sub>4</sub> in the same way to obtain the trimer P<sub>4</sub>=P<sub>4</sub>=P<sub>4</sub>, P<sub>12</sub> (D<sub>2d</sub>), Figure 5a, in an exothermic reaction, and P<sub>4</sub>=P<sub>4</sub>=P<sub>4</sub>=P<sub>4</sub>, P<sub>16</sub> (D<sub>2h</sub>), not shown, in an endothermic reaction, Table I. The probable reason for the destabilization of this tetramer, P<sub>16</sub>, is the occurrence of boat-shaped six-membered rings with some phosphorus lone pairs pointing at each other more than, e.g., in the dimer where bond angles allow the lone pairs to point into less crowded space.

Thus there is probably no stable polymeric form (=P<sub>4</sub>)<sub>∞</sub> as there is probably no (-P<sub>4</sub>-)<sub>∞</sub> with P<sub>4</sub> units linked by single bonds as discussed earlier.

**P<sub>8</sub> Units Linked by Two Single Bonds.** The hypothetical dimer of P<sub>4</sub>, P<sub>4</sub>=P<sub>4</sub> or P<sub>8</sub> (D<sub>2h</sub>), Figure 1g, may be stabilized by addition of another P<sub>4</sub> tetrahedron as discussed before or by isomerization to P<sub>8</sub> (C<sub>2v</sub>), Figure 1f, the most stable P<sub>8</sub> cluster. Again two bonds



**Figure 4.** Computed structures of phosphorus clusters containing PP double bonds: (a) P<sub>10</sub> (C<sub>2v</sub>), (b) P<sub>12</sub> (C<sub>2v</sub>) P<sub>2</sub>=P<sub>8</sub>=P<sub>2</sub>, (c) P<sub>10</sub> (C<sub>2v</sub>).



**Figure 5.** Computed structures of phosphorus clusters built from  $P_4$  and  $P_8$  units linked by two single bonds: (a)  $P_{12}$  ( $D_{2d}$ ), (b)  $P_{12}$  ( $C_s$ ), (c)  $P_{16}$  ( $C_s$ ), (d)  $P_{16}$  ( $C_{2h}$ ), (e)  $P_{24}$  ( $C_{2v}$ ).

have to be broken and two new bonds have to be formed.

As for  $P_4=P_4$ , one can stabilize  $P_8$  ( $C_{2v}$ ) by adding another  $P_4$  tetrahedron. The resulting molecule,  $P_{12}$  ( $C_s$ ), i.e.,  $P_8=P_4$ , Figure 5b, comes close to  $3P_4$  in stability at the SCF/SVP level, Table I, and is found to be more stable than  $3P_4$  at the MP2 level, Table III. The source of stabilization is the same as that in the formation of  $P_{10}$  ( $C_s$ ) (which we may also term  $P_8=P_2$ ) discussed earlier. Further addition of another  $P_4$  molecule to yield  $P_8=P_4=P_4$  (or  $P_{16}$  ( $C_s$ )), Figure 5c, proceeds almost isoenergetically; the corresponding molecules are 15 and 14 kJ/mol higher than  $nP_4$ , respectively, Table I.

$P_8=P_4=P_4$  can be greatly stabilized by the isomerization to  $P_8=P_8$  ( $P_{16}$  ( $C_{2h}$ )), Figure 5d, similar to the formation of  $P_8$  ( $C_{2v}$ ) from  $P_4=P_4$ .  $P_8=P_8$  is the most stable phosphorus cluster considered so far (in this work) and is considerably more stable than  $4P_4$  (by 109 kJ/mol at the SCF/SVP level), Table I. Properties of  $P_8=P_8$  are listed in Table VI and are available as supplementary material (NMR shifts).

To address the question if  $P_8=P_8$  continues to polymerize to form  $(=P_8)_\infty$ , we also calculated the trimer  $P_8=P_8=P_8$  or  $P_{24}$  ( $C_{2v}$ ), Figure 5e, Table I. Surprisingly we found  $P_8=P_8=P_8$  to be slightly less stable than  $P_8=P_8$ , with energies (relative to  $P_4$ ) of  $-23$  kJ and  $-27$  kJ per mole of  $P_4$ , respectively, Table I. This is again similar to the situation with the clusters  $P_8=P_2$  (or  $P_{10}$  ( $C_s$ ), Figure 4a) and  $P_2=P_8=P_2$  (or  $P_{12}$  ( $C_{2v}$ ), Figure 4b) where addition of a second  $P_2$  molecule to  $P_8=P_2$  does not lead to further gain in energy.

The energy of  $(=P_8)_\infty$  as calculated from  $P_8=P_8=P_8$  and  $P_8=P_8$

$$E(=P_8)_\infty - 2E(P_4) \approx E(P_8=P_8=P_8) - E(P_8=P_8) - 2E(P_4) = -27 \text{ kJ/mol} \quad (2)$$

is nevertheless below the energy of  $P_4$ , but it is above the energy of  $P_8=P_8$ .

**Alternating  $P_4$  and  $P_2$  Units Linked by Two Single Bonds.**  $P_4=P_2$  or  $P_6$  ( $C_{2v}$ ), Figure 1c, may be viewed as the monomeric building

block of a polymeric form of phosphorus. The first oligomers (without  $P=P$  double bonds) are  $P_4=P_2=P_4$  ( $P_{10}$  ( $C_{2v}$ )), Figure 6a, which is of comparable stability as  $P_4$ , Table I, and  $P_4=P_2=P_4=P_2=P_4$  ( $P_{16}$  ( $C_2$ )), Figure 6b. The latter is more stable than  $4P_4$  by 51 kJ/mol at the SCF/SVP level, Table I. Some calculated properties of these molecules are given in Table VI and as supplementary material.

A crude estimate for the stability of an infinite chain  $(=P_4=P_2)_\infty$  is obtained from the energy difference between  $P_4=P_2=P_4$  and  $P_4=P_2=P_4$ :

$$E(=P_4=P_2)_\infty - 1.5E(P_4) \approx E(P_4=P_2=P_4=P_2=P_4) - E(P_4=P_2=P_4) - 1.5E(P_4) = -49 \text{ kJ/mol} \quad (3)$$

which corresponds to  $-32$  kJ/mol per  $P_4$  unit. This hypothetical polymer is the energetically most stable form of phosphorus discussed up to this point.

**Alternating  $P_8$  and  $P_2$  Units Linked by Two Single Bonds and Related Clusters.** The stability of  $P_8=P_2$  ( $P_{10}$  ( $C_s$ )), Figure 4a, has been discussed before. It, too, may be viewed as a unit of a polymeric form of phosphorus,  $(=P_8=P_2)_\infty$ , of which the first oligomers (without  $PP$  double bonds) are  $P_8=P_2=P_8$  ( $P_{18}$  ( $C_{2v}$ )), Figure 6c, and  $P_8=P_2=P_8=P_2=P_8$  ( $P_{28}$  ( $C_{2v}$ )), Figure 6d. These are the most stable phosphorus clusters we found, Table I. Their properties, as far as we could calculate them, are given in Table VI and as supplementary material. From the energies of  $P_{28}$  and  $P_{18}$  we estimate the energy of the polymer:

$$E(=P_8=P_2)_\infty - 2.5E(P_4) \approx E(P_8=P_2=P_8=P_2=P_8) - E(P_8=P_2=P_8) - 2.5E(P_4) = -147 \text{ kJ/mol} \quad (4)$$

The clusters  $P_{18}$  ( $C_{2v}$ ) and  $P_{28}$  ( $C_{2v}$ ) are probably difficult to obtain (despite their stability relative to  $P_4$ ) because the hypothetical polymer  $(=P_8=P_2)_\infty$  has an even lower energy per phosphorus atom (eq 4). Any conditions under which  $P_{18}$  ( $C_{2v}$ ) and  $P_{28}$  ( $C_{2v}$ ) are formed would thus probably also promote the growth of longer chains. We note, however, that  $P_8=P_2=P_8$  and  $P_8=P_2=P_8=P_2=P_8$  are bent (and not linear structures in their equilibrium geometries),

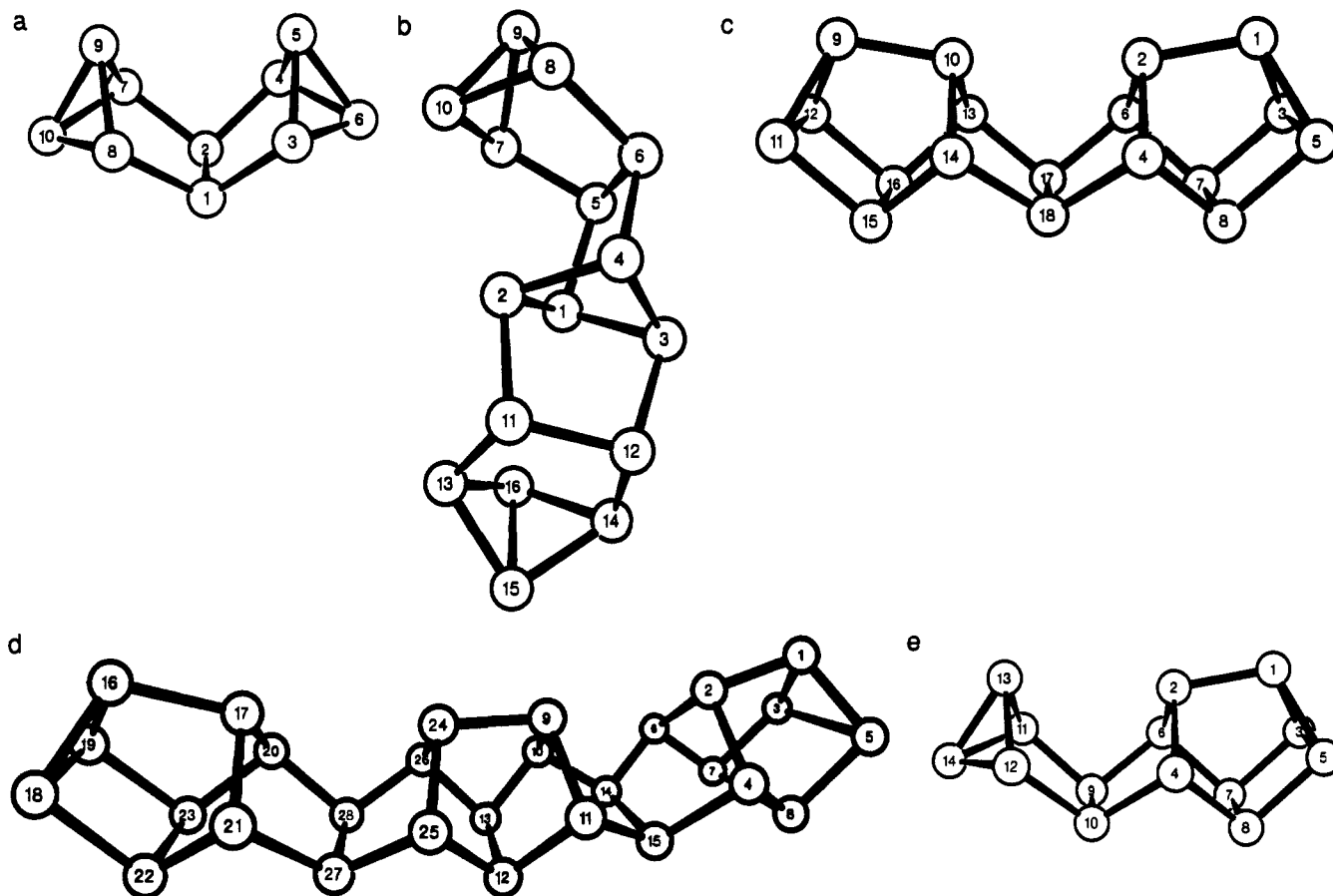


Figure 6. Computed structures of phosphorus clusters built from  $P_4$  or  $P_8$  units linked by  $P_2$  units: (a)  $P_{10}$  ( $C_{2v}$ ), (b)  $P_{16}$  ( $C_2$ ), (c)  $P_{18}$  ( $C_{2v}$ ), (d)  $P_{28}$  ( $C_{2v}$ ), (e)  $P_{14}$  ( $C_2$ ).

and regular chain growth would probably not lead to a simple lattice structure.

We also note the similarity between  $(P_8=P_2)_n=P_8$  and the building blocks of Hittorf's violet phosphorus<sup>4</sup> which contains  $(=P_8=P_2=P_9=P_2=)_n$  chains, with the  $P_9$  units interconnecting with other chains, building a complicated three-dimensional network. The  $P_9$  units probably straighten the otherwise bent  $=P_8=P_2=$  structures and thus allow linear chains with minimum strain. This has first been suggested in ref 4.

Other than with  $(=P_4=P_2=)_\infty$  the growth of  $(=P_8=P_2=)_\infty$  polymers cannot be nourished by a supply of  $P_8$  ( $C_{2v}$ ) molecules since they are significantly less stable than  $P_4$ . Fortunately, however, intermediate clusters like  $P_8=P_2=P_4$  (or  $P_{14}$  ( $C_2$ )), Figure 6e, can be expected to be very stable (with respect to  $P_4$ ), Table I.

**Other Clusters.** We studied two clusters which do not fit into any of the categories mentioned so far. The first of them is  $P_{10}$  ( $C_{2h}$ ), Figure 7a. Its energy is unfavorable, Table I. The other cluster is  $P_{16}=P_4$  ( $P_{16}$  ( $C_2$ )), Figure 7b, that is, a  $P_4$  tetrahedron added to the stable  $P_{12}$  ( $D_{3d}$ ) cluster, Figure 3c. There are, of course, three different kinds of bonds in  $P_{12}$  to add on, but we studied only the approach considered most likely which opens one of the three-membered rings in  $P_{12}$ . The addition reaction proves to be endothermic by 59 kJ/mol ( $P_{16}$ ).  $P_{12}$  ( $D_{3d}$ ) thus is probably kinetically stable against attack by  $P_4$ .

#### IV. Computed Properties and Accuracies

So far we have mainly discussed SCF energies obtained with an SVP basis set (for SCF/SVP optimized structures, of course). SVP is the smallest type of basis set for which reasonable results can be expected. We have performed additional SCF/TZDP calculations of equilibrium geometries for  $P_4$  and  $P_{12}$  ( $D_{3h}$ ) which result in only minor changes in structure constants, e.g., bond shortenings change by  $\leq 1$  pm.

The main source of error in computed structure constants thus arises from effects of electron correlation. The deviation between

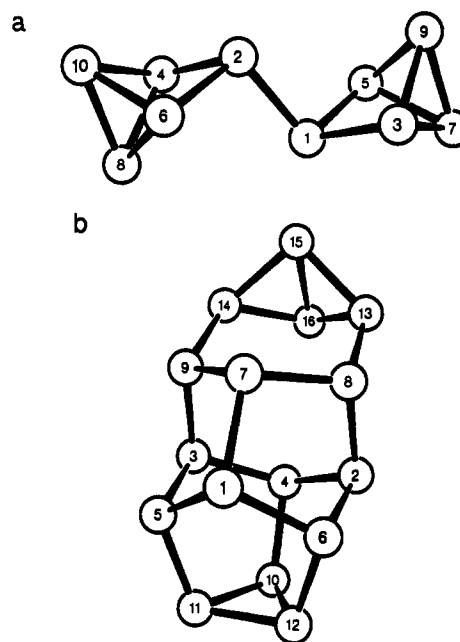
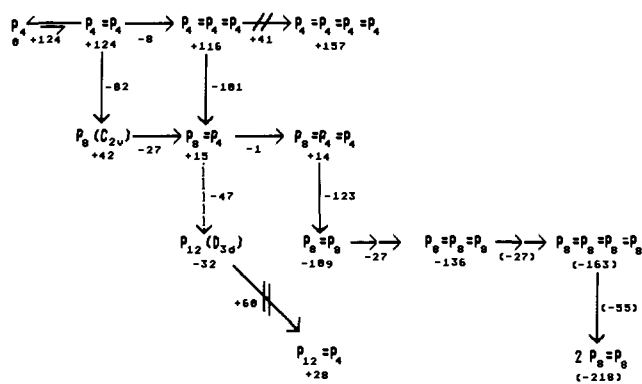


Figure 7. Computed structures of phosphorus clusters  $P_{10}$  and  $P_{16}$ : (a)  $P_{10}$  ( $C_{2h}$ ), (b)  $P_{16}$  ( $C_2$ ).

the experimental bond distance of  $P_4$ ,  $221 \pm 2$  pm<sup>1</sup> (incidentally virtually identical to the MP2/SVP value of 220.8 pm), and the SCF/SVP value, 218.9 pm, amounts to 2 pm. This indicates a typical error of 3 pm in computed bond distances, at least for the reasonably stable isomers with "normal" bonding situations. We likewise expect bond angles on the SCF/SVP level to be in error by typically up to  $3^\circ$ . This conclusion has been checked by an MP2/SVP treatment for  $P_{12}$  ( $D_{3d}$ ) documented in Table VI. The

Scheme I<sup>a</sup>

Reaction Scheme A

<sup>a</sup>A possible reaction scheme for the polymerization of phosphorus involving  $P_4$  only. Energies have been calculated at the SCF/SVP level of theory and are given in kJ/mol relative to the energy of  $n P_4$ ; energies in brackets are authors estimates.

deviations between SCF and MP2 structure constants are smaller than 3 pm and 1°, and it appears that electron correlation tends to shorten the shorter and to lengthen the longer bonds.

In Table III we have collected MP2/SVP energies and SCF/SVP zero point vibrational energies. In all cases listed only real frequencies were found and therefore the corresponding structures are local minima on the SCF/SVP surface. In Table IV we report for a few selected cases SCF and MP2 energies obtained with the extended TZDP basis, at the SCF/SVP geometries, as a further check. The following trends can be extracted from these results, Tables III and IV:

(i) With the SVP basis one overestimates the stability of the larger clusters relative to the extended TZDP basis by about  $10 \pm 3$  kJ per mole of  $P_4$  on the SCF level. This trend could be attributed to basis set superposition effects present with the smaller SVP basis or the fact that the SVP basis underestimates the stability of  $P_4$ .

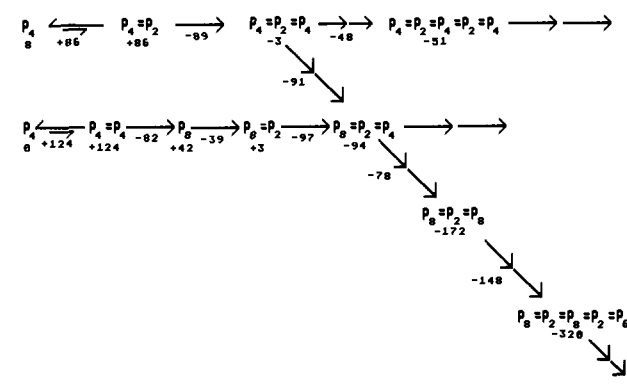
(ii) MP2/SVP contributions always stabilize the more stable of the larger clusters by roughly  $21 \pm 5$  kJ per mole of  $P_4$ . As far as can be seen from the few results — for  $P_8 (C_{2v})$  and  $P_{12} (D_{3d})$  — the MP2 stabilization of the more stable larger clusters is underestimated by the SVP basis (not unexpectedly) as compared to the TZDP basis.

(iii) The two above comments suggest that the MP2/SVP results, Table III, may slightly overestimate the stability of the (more stable) larger clusters.

The computed SCF/SVP vibrational wavenumbers of  $P_4$  (in comparison to experiment<sup>17</sup>) are, in  $\text{cm}^{-1}$ ,  $e$  403 (360),  $t_2$  511 (450), and  $a_1$  672 (600). SCF/SVP overestimates the frequencies by 12–14%, and this may be expected to hold also for the stiffer modes of the other clusters, available as supplementary material.

It is hard to estimate errors of computed NMR chemical shifts<sup>18</sup> (available as supplementary material). We can only offer our personal judgement that deviations from experiment should typically be less than 30 ppm for the TZDP basis (mainly effects of electron correlation), provided solvent effects are negligible. NMR shieldings,  $\sigma$ , obtained with the smaller DZP basis are systematically larger than for the TZDP basis. The deviation appears to increase if  $\sigma$  decreases. Computed shielding constants show an obvious correlation with the sum of bond angles of corresponding phosphorus atoms: the smaller the sum of bond angles the larger the shielding and the smaller the chemical shift.

The above comments in mind we report the most important structure constants in Table VI. SCF/SVP vibrational frequencies and IR intensities are available as supplementary material (or on request from the authors) for all cases for which the ZPVE has been given in Table III.

(17) Ozin, G. A. *Chem. Commun.* 1969, 1325.(18) Bouman, T. D.; Hansen, A. E. *Chem. Phys. Lett.* 1990, 175, 292.Scheme II<sup>a</sup>

Reaction Scheme B

<sup>a</sup>A possible reaction scheme for the polymerization of phosphorus involving  $P_2$  and  $P_4$ . Energies have been calculated at the SCF/SVP level of theory and are given in kJ/mol relative to the energy of  $n P_4$ ; energies in brackets are authors estimates.

## V. Discussion

From the data gathered, a coherent picture emerges as to how white phosphorus could react to form larger clusters and finally polymeric forms of phosphorus (red phosphorus). Two hypothetical reaction pathways are presented in Schemes I and II. They represent possible cascades of increasingly stable intermediate aggregates. The formation of the first intermediate (start up reaction), however, is always endothermic, well in accord with the kinetic stability of white phosphorus.

Scheme I involves only reactions where two bonds are broken and two bonds are formed in each step. This pathway would possibly yield two stable clusters  $P_8 = P_8$ , Figure 5d, and  $P_{12} (D_{3d})$ , Figure 3b. The latter cluster, however, can be derived from  $P_8 = P_4$ , Figure 5b, only by breaking three bonds.

Scheme II suggests  $P_2$  as an intermediate, at least in a start up reaction. No islands of particularly stable oligomers exist. Instead there is always an energy gain by further cluster growth, yielding a variety of inhomogeneous polymeric phosphorus chains of which  $(=P_4=P_2=)_\infty$  and  $(=P_8=P_2=)_\infty$  are two well-defined limiting cases. Other possible repeating units comprise  $=P_8=P_8=P_2=$  and  $=P_{10}=P_2=$  where the  $P_{10}$  subunit is derived from  $P_{14}R_4$ .<sup>19</sup> In the chains there may be further interspersed structural subunits like  $P_7$ , as in  $(Ph_4P)_2P_{16}$ ,<sup>6,20</sup> or  $P_9$ , as in Hittorf's violet phosphorus,<sup>4</sup> or various (substituted) phosphanes<sup>5,21</sup> thus allowing for cross-links between chains.

## VI. Conclusions

The application of ab initio methods presented in this work has for the first time shed some light on phosphorus chemistry between  $P_8$  and  $P_\infty$ , which has been a terra incognita so far. This effort involved extensive calculations on 39 species (32 phosphorus clusters and 7 phosphanes) ranging in size up to  $P_{28}$  (the largest cluster previously tackled by ab initio methods was  $P_8$ ).<sup>2</sup> In the choice and design of clusters and their structural features we have been led by chemical intuition and cannot claim completeness. Although further treatments will certainly extend our knowledge, these will hardly affect the basic result of the present study: the first characterization of phosphorus clusters which are energetically stable with respect to decomposition into  $P_4$ , which in turn allow one to estimate the stability of possible polymers, eqs 1–4.

A wealth of data has been obtained from which a consistent picture of phosphorus emerges: an old hypothesis on structure and formation of red phosphorus has been refuted,<sup>14</sup> and new hypotheses have been suggested which have passed the tests ab

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initio quantum chemistry can provide by itself at present (a detailed investigation of reactions would require considerably larger efforts). Two medium-size phosphorus clusters,  $P_{12}$  ( $D_{3d}$ ) and the  $P_8=P_8$  structure of  $P_{16}$  ( $C_{2h}$ ), have been established as particularly stable under appropriate conditions.

The calculated properties (equilibrium structures, IR and Raman spectra, and NMR shieldings) should allow experimentalists to positively identify some of the clusters or the structural units in red phosphorus. The expected range of error for calculated bond lengths is 3 pm, for bond angles  $3^\circ$ , for (stiff) vibrational frequencies 10–15% (systematically too high), and around 30 ppm for relative chemical shieldings. These estimates arise from comparison with experiment for  $P_4$  and from the fact that SCF/TZDP geometries vary by only 1 pm from SCF/SVP for  $P_4$  and  $P_{12}$ . Since the stable clusters form a relatively uniform class of compounds (PP single bond distances are between 220 and 231 pm throughout), it may be safely expected that trends in computed properties are reliably described.

After submission of this manuscript, a density functional study on phosphorus clusters  $P_9$  to  $P_{11}$  was published.<sup>22</sup> The cluster  $P_{10}$  ( $C_{2v}$ ), Figure 6a, which according to our study is the most stable  $P_{10}$  isomer, has not been found in ref 22.

**Acknowledgment.** We are indebted to Dr. F. Haase for performing the MP2 geometry optimization on  $P_{12}$  and to Professor M. Baudler for making unpublished material available to us. This work has been supported by the Fonds der Chemischen Industrie.

**Supplementary Material Available:** SCF/SVP vibrational frequencies for all molecules listed in Table III, if zero point vibrational energies are given, and NMR shielding constants  $\sigma$  and chemical shifts  $\delta$  (in ppm) calculated with TZDP or DZP basis sets at the SCF/SVP geometries for the clusters depicted in Figures 1a, 1f, 1h, 3b, 3e, 4a, 5d, and 6a–6e (5 pages). Ordering information is given on any current masthead page.

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## $\pi$ -Bond Strengths of $H_2X=YH_2$ : X = Ge or Sn, and Y = C, Si, Ge, or Sn

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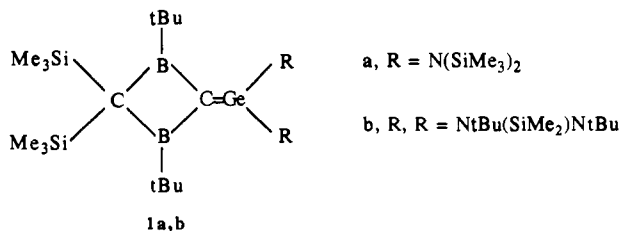
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**Abstract:** The molecular structures and  $\pi$ -bond strengths are determined using both MP2 and MCSCF + CI energies for a series of  $H_2X=YH_2$  compounds, where X = Ge or Sn and Y = C, Si, Ge, or Sn. These strengths are estimated both by evaluating the rotation barriers and by investigating the appropriate thermochemical cycles. The results show that C > Si ~ Ge > Sn in their ability to form  $\pi$ -bonds.

### I. Introduction

Recently there has been considerable interest in the molecular and electronic structure and the reactivity of compounds containing a double bond between group IVA elements. But, while the double bonds in ethylene, disilene, and silaethylene have been well-characterized by both experiment and theory (see, for instance, refs 1–5), the double bonds formed with germanium and tin have only recently been examined. Several reviews have been written on the subject of Ge and Sn double bonds.<sup>6</sup> Many of the species which contain double bonds to these elements are transient reactive intermediates. However, some have been isolated.

Through the use of large, bulky groups for steric and electronic stabilization, three germenes ( $R_2Ge=CR'_2$ ) were isolated in 1987.<sup>7,8</sup> (Until then, germenes had been seen only as transient species.<sup>9–12</sup>) At that time, Berndt and co-workers<sup>7</sup> synthesized germenes **1a** and **1b**.



These stable germenes were characterized by both NMR and X-ray diffraction techniques. The  $Ge=C$  bond length was de-

termined to be 1.827 Å, with an average twist angle of  $36^\circ$  about the  $GeC$  bond. In addition, the local structure about the Ge and

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